

fshift_increasing^{4,23}

$\forall n:\mathbb{N}, x:\mathbb{Z}, f:(\mathbb{N}_{< n} \rightarrow \mathbb{Z}). \text{ increasing}(f;n) \Rightarrow 0 < n \Rightarrow x < f(0) \Rightarrow \text{increasing}(\text{fshift}(f;x);n+1)$